

# Energy Efficient Inter-Frequency Small Cell Discovery in Heterogeneous Networks

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**Abstract**—In this paper, using stochastic geometry, we investigate the average energy efficiency (AEE) of the user terminal (UT) in the uplink of a two-tier heterogeneous network (HetNet), where the two tiers are operated on separate carrier frequencies. In such a deployment, a typical UT must periodically perform inter-frequency small cell discovery (ISCD) process in order to discover small cells in its neighborhood and benefit from the high data rate and traffic offloading opportunity that small cells present. We assume that the base stations (BSs) of each tier and UTs are randomly located and we derive the average ergodic rate and UT power consumption, which are later used for our AEE evaluation. The AEE incorporates the percentage of time a typical UT missed small cell offloading opportunity as a result of the periodicity of the ISCD process. In addition to this, the additional power consumed by the UT due to the ISCD measurement is also included. Moreover, we derive the optimal ISCD periodicity based on the UT's average energy consumption (AEC) and AEE. Our results reveal that ISCD periodicity must be selected with the objective of either minimizing UT's AEC or maximizing UT's AEE.

**Index Terms**—Heterogeneous cellular network, stochastic geometry, fractional power control, small cell discovery, energy efficiency.

## I. INTRODUCTION

To meet the exponentially growing capacity demands, the future of cellular networks is marked by heterogeneous deployments consisting of legacy macro cells with overlaid or underlaid small cells [1]–[7]. Small cell enhancement could either be a scenario where different frequency bands are separately allocated to the small cell and macro cell layers or co-channel deployment scenario, where the small cell and macro cell layers share the same carrier [2]–[4], [8]. It is expected that in the future, small cells will operate on dedicated higher frequency bands, such as 3.5, 5 and beyond 5 GHz bands, where new licensed spectrum is expected to be available [1], [4], [8]. Since small cells have smaller coverage footprint, they do not suffer from the high propagation loss which such band causes to macro cells. Furthermore, cross-tier interference is avoided by operating the small cells on the dedicated higher

frequency bands, thus leading to an improvement in spectral efficiency [4]. The use of such bands for small cell can also lead to a significant increase in capacity, since they can offer larger bandwidths. Hence, small cells can provide high data rate to hot spots while also offering traffic offloading opportunity, which can be boosted by incorporating range expansion bias [5], [6].

In the deployments where different frequency bands are separately allocated to the small cell and macro cell layers, user terminals (UTs) connected to the macro cell must periodically scan for suitable small cells in their neighborhood in order to benefit from the high data rate and the traffic offloading opportunity which such offers. This can result in significant energy consumption to the UT. The power limited nature of the UTs is major challenge in enabling truly broadband networks, hence; energy efficient discovery of small cells has been identified by 3GPP as an important technical issue in carrier-frequency separated deployments [9]. Various inter-frequency small cell discovery (ISCD) mechanisms have been studied in literature. Some of the proposed solutions for enhancing ISCD include: UT speed based measurement triggering [10], [11], relaxed inter-frequency measurement gap [12], proximity based ISCD [11], small cell signal based control measurement and small cell discovery signal in macro layer [3], [13]. A common feature in all the ISCD mechanisms is the periodic inter-frequency scanning and measurement by the UT, which results in significant UT energy consumption.

For a given small cell deployment density and UT speed, low ISCD periodicity (i.e. high scanning frequency) can result in increased small cell offloading opportunity, thus enhancing the capacity and coverage. However, this can also lead to higher UT power consumption due to the high scanning frequency. Meanwhile, the UT's transmit power can be reduced as a result of offloading to the small cells where lower transmit power is required due to smaller cell radii. On the other hand, high ISCD periodicity (i.e. low scanning frequency) can lead to the UT missing small cell offloading opportunity, thus resulting in a potential decrease in capacity. Most prior work on ISCD in literature have focused only on the effect of ISCD periodicity on scanning power without evaluating the impact of UT transmit power reduction when offloading to the small cells [10]–[12], [14]. In [14], a mobility aware handover scheme for HetNets consisting of WiMAX and WiFi networks was proposed. In their proposed scheme the UT intelligently selects a subset of the network to be scanned, thus saving UT energy consumption. Mobility based small-cell search has been identified in [10], [11] as an approach that works well

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This work was made possible by NPRP grant No. 5-1047-2437 from the Qatar National Research Fund (a member of The Qatar Foundation). The statement made herein are solely the responsibility of the authors. More information about this project can be found at [www.qson.org](http://www.qson.org).

within the LTE-A deployment. It has also been shown in [11] that this approach can provide a savings of up to 99% in UT battery power consumption. Only recently, [15] considered UT transmit power reduction as a result of offloading to the small cell in their evaluation. However, the energy efficiency of this scheme is yet to be investigated. Using stochastic geometry, an analytical framework was proposed in [16] to analyze the trade-off between traffic offloading from the macro cells and the energy consumption of cognitive small cell access points.

In this paper, we investigate the average energy efficiency (AEE) of a typical UT in the uplink of HetNet, where the small cells are deployed on carrier frequency other than that of the serving macro cell and an ISCD scheme is utilized by the UT. The AEE of a communication system is the average amount of bits that can be delivered per joule consumed to do so, i.e. the ratio of the average ergodic rate to the total power consumed [17], [18]. The ergodic rate and the power consumed by a typical UT depend on its association, which could be with either a macro cell or small cell. Hence, the AEE of a typical UT in a HetNet must be obtained by taking the following into consideration: its average power consumption in the macro cell and small cell layers; its average achievable rate in the macro cell or small cell layers; the percentage of time it missed small cell offloading opportunity as a result of the ISCD periodicity and; the additional power it consumes due to ISCD measurement. We model the BS locations as random and drawn from spatial stochastic process, such as homogeneous Poisson point process (PPP). In actual deployment, small cells are usually unplanned; hence, they are well modeled by the spatial random process [19]–[22]. On the other hand, modeling macro cell BSs as PPP provide lower bounds to the average rate and coverage probability of real deployment [23]. Repulsive point process such as Matérn hard core point process (HCPP), which reflect the minimum separation distance between BSs, provides a more realistic model but at the expense analytical tractability [24], [25].

In Section II, we first present the HetNet system model, which incorporates a range extension bias scheme to boost the small cell offloading potential. Next, we present the probability of UT's association to a tier and the probability density function (PDF) of the statistical distance between a typical UT and it serving BS, which later serves as a basis for our derivations. In Section III, we present the ISCD process and its implication in terms of the percentage of time a typical UT missed small cell offloading opportunity. In Section IV, we derive the average UT power consumption and ergodic rate per tier, which are later used in Section V to evaluate its AEE. We derive both the ideal and the realistic AEE of the typical UT in the uplink of the carrier frequency separated HetNet. The ideal AEE is based on an ideal UT association, where the UT associates with the BS (small or macro cell) with the maximum biased received power [6], [22], [26], [27]. On the other hand, the realistic AEE is based on a realistic UT association, where UT association with the small cell is also dependent on the periodicity of the ISCD [11], [12], [15]. In Section VI, we first utilize a polynomial fitting method to approximate the percentage of time the typical UT missed small cell offloading opportunity as a function of ISCD periodicity, for

a fixed UT speed and small cell density. Subsequently, by using the approximated function, we derive the average energy consumption (AEC) and AEE optimal ISCD periodicities, for a fixed UT speed and small density. Numerical results are presented in Section VII. Results show that significant savings in the UT's AEC can be achieved by utilizing the optimal ISCD periodicity. Furthermore, ISCD periodicity should be set based on the target objective, which could be towards either AEC minimization or AEE maximization. Finally, conclusions are drawn in Section VIII. A preliminary version of this work has been reported in [28]. Herein, we have considered the interference limited deployment with a cell range extension bias scheme and UT power control.

## II. SYSTEM MODEL

We consider a HetNet deployment which is made up of 2 tiers of BSs. The first tier represents macro cell layer while the second tier represents small cell layer. We consider that each tier operates on a different carrier frequency and that each tier is identified by its biasing factor, pathloss exponent and, its BSs transmit power and spatial density. The positions of BSs in the  $j^{\text{th}}$  tier are modeled according to a homogeneous PPP  $\Phi_j$  with density  $\lambda_j$ . Furthermore, a fully loaded network with one active uplink user per channel is assumed with the UTs locations approximated by a homogeneous PPP  $\Phi^{(u)}$  with density  $\lambda^{(u)}$ , which is independent of  $\{\Phi_j\}_{j=1,2}$ . It is also assumed that the density of the UTs is high enough such that each BS in the network have a least one UT served per channel. We consider that the received signals in the  $j^{\text{th}}$  tier are subject to pathloss, which we model using the pathloss exponent  $\alpha_j$ . The random channel variation is modeled as Rayleigh fading with unit mean. We consider that an orthogonal multiple access scheme is utilized within each cell, such that there is no intra-cell interference. Furthermore, each of the BSs in the  $j^{\text{th}}$  tier transmit the same power, i.e.  $P_j$ , while the noise power is assumed to be  $\sigma^2$ . In order to evaluate the average UT transmit power, ergodic rate and AEE, we shift all point process such that a typical UT lies at the origin. Regardless of this shift, the homogeneous PPP distribution of the BSs remains preserved.

*UT Association:* Given that  $k \in \{1, 2\}$  denotes the index of the tier with which a typical user is associated and  $|S_{ki}|$  is the distance between the typical UT, i.e., the origin and BS  $i \in \Phi_k$ . Also the distance between the typical UT and the nearest BS in the  $j^{\text{th}}$  tier is denoted by  $D_j$ . We consider that the UT is associated with a cell based on the maximum biased-received-power (BRP), i.e., the UT associates with the strongest BS in terms of the long-term averaged BRP [22]. The BRPs to the typical UT from the nearest BS in the  $j^{\text{th}}$  tier can be expressed as

$$P_{r,j} = P_j L_0 \left( \frac{D_j}{d_0} \right)^{-\alpha_j} \beta_j, \quad (1)$$

where  $L_0$  denotes the pathloss at a reference distance  $d_0$  and  $\beta_j$  is the biasing factor, which is the same for all the BS in the  $j^{\text{th}}$  tier. The biasing factor,  $\beta_j$ , can be used to adjust the tier's selection of UTs to allow for effective load balancing. Note

that  $\{\beta_j\}_{j=1,2} = 1$  denotes the conventional cell association, where the UT connects to the BS that offers the highest average received power to the UT.

*Distribution of the Distance between UT and Serving BS:* It has been shown in [22, Lemma 3] that the probability density function (PDF),  $f_{X_k}(x)$ , of the distance  $X_k$  between a typical UT and its serving BS in the  $k^{\text{th}}$  tier based on the maximum BRP can be expressed as

$$f_{X_k}(x) = \frac{2\pi\lambda_k}{\mathcal{A}_k} x \exp \left\{ -\pi \sum_{j=1}^2 \lambda_j \left( \widehat{P}_j \widehat{\beta}_j \right)^{2/\alpha_j} x^{2/\alpha_j} \right\}, \quad (2)$$

where  $\mathcal{A}_k$ , which is defined subsequently in (3), is the idealistic probability of the typical UT associating to the  $k^{\text{th}}$  tier.

*Idealistic Probability of UT Association to a Tier:* In the ideal settings, the UT associates with BSs based on the maximum BRP. In case of UT mobility, handover signaling overhead and other mobility related overheads are not considered. Furthermore, all handover associated time, such as handover preparation time, handover execution time, time to trigger and the ISCD measurement time, are all equal to zero. Hence, in an ideal two-tier HetNet, the idealistic probability that a typical UT is associated with a BS of the  $k^{\text{th}}$  tier can be expressed according to [22, Lemma 1] as

$$\mathcal{A}_k = 2\pi\lambda_k \int_0^\infty r \exp \left\{ -\pi \sum_{j=1}^2 \lambda_j \left( \widehat{P}_j \widehat{\beta}_j \right)^{2/\alpha_j} r^{2/\alpha_j} \right\} dr, \quad (3)$$

where  $\widehat{P}_j \triangleq \frac{P_j}{P_k}$ ,  $\widehat{\beta}_j \triangleq \frac{\beta_j}{\beta_k}$ ,  $\widehat{\alpha}_j \triangleq \frac{\alpha_j}{\alpha_k}$ . It follows that in an ideal UT association, the probability that a typical UT associates with a tier is dependent on the BSs transmit powers,  $\{P_j\}_{j=1,2}$ , densities  $\{\lambda_j\}_{j=1,2}$ , and bias factors  $\{\beta_j\}_{j=1,2}$ . Moreover,  $\mathcal{A}_k$  can be interpreted as the average fraction of time that a typical UT is connected to the BSs belonging to the  $k^{\text{th}}$  tier [26]. Given the total time  $T \rightarrow \infty$ , the average time that the typical UT spends in the coverage of the macro cell (tier 1) and small cell (tier 2) can be expressed as

$$\begin{aligned} T_1 &= \mathcal{A}_1 T & \text{and} \\ T_2 &= \mathcal{A}_2 T \end{aligned}, \quad (4)$$

respectively, where  $\mathcal{A}_k, \forall k = \{1, 2\}$  is defined in (3).

*Realistic UT Association:* In the realistic setting, a typical UT that is connected to the macro cell must periodically scan for suitable inter-frequency small cell (i.e. small cell with higher BRP) before it can discover and offload its traffic (i.e. change association) to such small cell. Hence, ISCD scanning and measurements are performed by UTs when associated with the macro cell, at a network or UT specified periodicity. As a result of the scanning periodicity and UT mobility, there exists a fraction of time,  $\mathcal{X}$ , that the typical UT would miss small cell offloading opportunity. This implies that on the average, the typical UT becomes connected to the macro cell for  $\mathcal{X}$  more fraction of time that the small cell provides the maximum BRP. Hence, the average realistic time that the typical UT spends in the macro cell coverage can be expressed from (4) as

$$\widetilde{T}_1 = \mathcal{A}_1 T + \mathcal{A}_2 T \mathcal{X} = T(\mathcal{A}_1 + \mathcal{A}_2 \mathcal{X}). \quad (5)$$

Similarly, the average realistic time that the typical UT spends in the small cell coverage can be expressed as

$$\widetilde{T}_2 = \mathcal{A}_2 T - \mathcal{A}_2 T \mathcal{X} = (1 - \mathcal{X}) \mathcal{A}_2 T. \quad (6)$$

### III. INTER-FREQUENCY SMALL CELL DISCOVERY (ISCD)

A UT connected to the macro cell periodically scans its neighbourhood to discover surrounding small cells. It also performs inter-frequency measurements to ensure that it can connect to another network when it finds a small cell with a higher BRP. The energy consumed for one inter-frequency small cell search can be expressed as

$$E_t = P_m T_m, \quad (7)$$

where  $T_m$  is the duration of the measurement and  $P_m$  is the power consumed by the UT for the measurement. For a given deployment density,  $\lambda_j$ , having a high scanning frequency results in a faster discovery of small cells and hence, increased small cell offloading opportunity, which leads to increase in system level capacity. However, high scanning rate implies an increase in UT's power consumption. On the other hand, reducing the scanning frequency results in the UT missing small cell offloading opportunity, thus, leading to a decrease in system level capacity. Also, the typical UT can significantly reduce its transmit power when connected to the small cells. Consequently, there exists a scanning frequency,  $\widehat{V}^*$ , that achieves optimal performance in terms of average UT energy consumption. If the scanning frequency is less than  $\widehat{V}^*$ , the small cells are not discovered on time, hence excessive UT energy consumption as the UT spends more time in macro cell coverage. On the other hand, excessive energy will be consumed in the search process if the scanning frequency exceed  $\widehat{V}^*$ . The impact of the ISCD frequency,  $\widehat{V}$ , or ISCD periodicity,  $V = \frac{1}{\widehat{V}}$ , can be modelled in terms of the percentage of time the UT missed small cell offloading opportunity,  $\mathcal{X}$ , as explained in the following.

Consider a typical UT moving according to a random direction mobility model with wrap around [29], [30]. The typical UT moves at a constant speed  $\theta$  on  $[0, 1)$  according to the following mobility pattern: A new direction or orientation is selected from  $(0, 2\pi)$  after the UT moves in a particular direction or orientation for a duration  $\varsigma$ , hence, the selection of the  $n^{\text{th}}$  direction initializes the  $n^{\text{th}}$  movement of the UT. The duration of each movement  $\varsigma$  is obtained as the time duration for the UT to move (at a constant speed  $\theta$ ) between two farthest points in the HetNet's coverage. In order to obtain  $\mathcal{X}$ , for a given UT speed, small cell density and ISCD periodicity  $V = \frac{1}{\widehat{V}}$ , we utilize the current 3GPP standard inter-frequency measurement of 40 ms as our benchmark. For the  $n^{\text{th}}$  movement with duration  $\varsigma$ , we estimate the time duration that the UT spends in the coverage of the small cell, based on ISCD periodicity  $V$  and the standard inter-frequency measurement of 40 ms, denoted by  $\varsigma_V^n$  and  $\varsigma_{40\text{ms}}^n$ , respectively. Hence, the average percentage of time the UT missed small cell offloading opportunity,  $\mathcal{X}$ , for a fixed UT speed,  $\theta$ , and small cell density  $\lambda_2$ , can be expressed as

$$\mathcal{X} = 1 - \mathbb{E} \left[ \frac{\varsigma_V^n}{\varsigma_{40\text{ms}}^n} \right], \quad (8)$$

where  $\mathbb{E}$  is the expectation operator.

In Fig. 1, we plot the percentage of time the UT missed small cell offloading opportunity,  $\mathcal{X}$ , against the ISCD periodicity,  $V = \frac{1}{\widehat{V}}$  for UT speed,  $\theta = 3, 10, 20, 30$  and 120 km/hr,

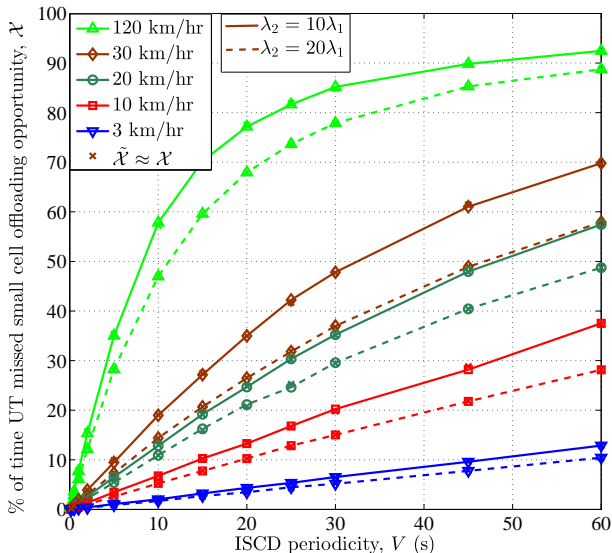


Fig. 1. Percentage of missed small cell offloading opportunity versus small cell discovery periodicity for various UT speed,  $\beta_1 = \beta_2 = 1$ ,  $\lambda_1 = \frac{1}{\pi 400^2 \text{m}^2}$ ,  $\lambda_2 = 10\lambda_1$  and  $20\lambda_1$ ,  $P_1 = 46$  dBm,  $P_2 = 26$  dBm and  $\alpha_1 = \alpha_2 = 4$ .

macro cell density  $\lambda_1 = \frac{1}{\pi 400^2 \text{m}^2}$ , small cell density  $\lambda_2 = 10\lambda_1$  and  $20\lambda_1$ , macro cell BS transmit power  $P_1 = 46$  dBm, small cell BS transmit power  $P_2 = 26$  dBm and pathloss exponent  $\alpha_1 = \alpha_2 = 4$ . It is obvious that if the scanning frequency is increased, the UT would miss the small cell offloading opportunity for a lesser time since the discovery process takes place more frequently at the time instance when the typical UT is in the coverage of the new small cell in its path. Also increasing the small cells density results in less likelihood for the typical UT to miss the small cell offloading opportunity. In addition, as the UT speed increases, the UT moves more quickly through the coverage of the small cell, hence an increase in the likelihood that the UT would miss the small cell offloading opportunity. Consequently, as the UT speed increases, the percentage of time that the typical UT missed the small cell offloading opportunity increases for any given ISCD periodicity, as illustrated in Fig. 1

#### IV. METRICS FOR ENERGY EFFICIENCY EVALUATION

Let  $\mathcal{R}$  (bit/s) be the achievable rate and  $\mathcal{P}_T$  be the total power consumed for transmitting data at this rate, then, the AEE can be expressed in terms of the bit-per-Joule as  $\mathcal{C}_J = \mathcal{R}/\mathcal{P}_T$ . Hence both the power consumption model and the achievable rate are essential in obtaining the AEE of a communication system.

##### A. UT Power Consumption Model

The AEE of a communication system is closely related to its total power consumption. The power consumed by the UT is made up of the transmit power and the additional circuit power incurred during transmission, which is independent of the transmission rate [31], [32]. If we denote the circuit power

as  $P_c$ , the overall power consumption of the typical UT at a distance  $x$  from its serving BS can be expressed as

$$\mathcal{P}_{T_x} = \Delta P_x^U + P_c, \quad (9)$$

where  $P_x^U$  is the transmission power of the typical UT,  $\Delta$  quantifies the UT power amplifier efficiency and it depends on the implementation and design of the transmitter [32].

*Average UT Transmit Power in a Tier:* Considering that the UT utilizes a distance-dependent fractional power control, hence the transmission power at a distance  $x$  to the BS in the  $k^{\text{th}}$  tier,  $P_x^U$ , is of the form  $P_k^0 x^{\alpha_k \tau_k}$ , where  $P_k^0$  is a parameter related to target mean received power (which is user or network specific) in the  $k^{\text{th}}$  tier, and  $\tau_k \in [0, 1]$  is the power control factor in the  $k^{\text{th}}$  tier. Therefore, as the typical UT moves closer to its associated BS, the transmit power required to achieve the target received signal power at the BS decreases. Hence, having smaller cells, where the UT can be closer to their serving BS as opposed to the traditional macro deployment, is expected to yield a reduction in the transmission power. This is an important consideration in power limited devices such as the battery powered mobile devices. The average transmit power of a typical UT in a tier is obtained by averaging  $P_x^U$  over the distance  $x$  (i.e., over the  $k^{\text{th}}$  tier) and is thus expressed as

$$\begin{aligned} P_k^U &= \mathbb{E}_x [P_k^0 x^{\alpha_k \tau_k}] \\ &= \int_0^\infty P_k^0 x^{\alpha_k \tau_k} f_{X_k}(x) dx \\ &\stackrel{(a)}{=} \frac{2\pi\lambda_k P_k^0}{\mathcal{A}_k} \int_0^\infty x^{(1+\alpha_k \tau_k)} \exp\left\{-\pi \sum_{j=1}^2 \lambda_j (\hat{P}_j \hat{\beta}_j)^{2/\alpha_j} x^{2/\alpha_j}\right\} dx \end{aligned} \quad (10)$$

where (a) follows from (2). If  $\alpha_j = \alpha$ ,  $\forall \{j = 1, 2\}$ , the average transmit power of the typical UT over the  $k^{\text{th}}$  tier is simplified according to [33, pp. 337] as

$$P_k^U = \frac{\pi \lambda_k P_k^0 \Gamma\left(1 + \frac{\alpha \tau_k}{2}\right)}{\mathcal{A}_k \left[\pi \sum_{j=1}^K \lambda_j (\hat{P}_j \hat{\beta}_j)^{2/\alpha}\right]^{(1 + \frac{\alpha \tau_k}{2})}} \quad (11)$$

where  $\Gamma$  denotes Gamma function. For the case without power control, i.e.  $\tau_k = 0$ , the average transmit power simplifies to  $P_k^0$  in (10) and (11), respectively. Consequently, the average overall power consumption of the UT in the  $k^{\text{th}}$  tier can be obtained as

$$\bar{\mathcal{P}}_{T_k} = \Delta P_k^U + P_c. \quad (12)$$

##### B. Average Ergodic Rate of a Typical UT in a Tier

The associated signal-to-interference-plus-noise ratio (SINR) at the BS in the  $k^{\text{th}}$  tier, which is at a random distance  $x$  from the typical UT can be expressed as

$$\text{SINR}_k(x) = \frac{h_{k,0} P_k^0 x^{\alpha_k (\tau_k - 1)}}{\sum_l h_{k,l} P_k^0 |Y_{k,l}|^{\alpha_k \tau_k} |V_{k,l}|^{-\alpha_k} + \sigma^2}, \quad (13)$$

where  $h_{k,0}$  is the exponentially distributed channel gain with mean  $\mu^{-1}$  from the typical UT,  $|Y_{k,l}|$  is the distance from each interfering UT to their serving BS in the  $k^{\text{th}}$  tier,  $|V_{k,l}|$

is the distance from the interfering UT to the BS serving the typical UT in the  $k^{\text{th}}$  tier, and  $h_{k,l}$  represents the exponentially distributed channel power from  $l^{\text{th}}$  interfering UT. Note that there is no inter-tier interference since both tiers operate on separate carrier frequencies. In addition, an orthogonal multiple access is also considered in each cell.

In order to derive the average ergodic rate of a randomly located UT in the  $k^{\text{th}}$  tier, we consider that the UT is associated with the BS with the maximum BRP. We then follow the same approach used in deriving the average UT transmit power in a tier. Firstly, the ergodic uplink rate of a typical UT at a distance  $x$  from its serving BS in the  $k^{\text{th}}$  tier is obtained. Thereafter, the ergodic uplink rate is then averaged over the distance  $x$  (i.e. over the  $k^{\text{th}}$  tier). The average ergodic rate of the  $k^{\text{th}}$  tier in the uplink channel is thus defined as

$$\mathcal{R}_k \triangleq \mathbb{E}_x [\mathbb{E}_{\text{SINR}_k} [\ln(1 + \text{SINR}_k(x))]]. \quad (14)$$

Contrarily to [34] where the average ergodic rate was obtained based on a fixed minimum distance for the interfering UT, we define the average ergodic rate which is without such limitation in the following theorem.

*Theorem IV.1:* The average ergodic uplink rate of a typical UT associated with the  $k^{\text{th}}$  tier is

$$\mathcal{R}_k = \frac{2\pi\lambda_k}{\mathcal{A}_k} \int_0^\infty \int_0^\infty x \exp\left\{-\frac{e^t-1}{\text{SNR}} - \pi \sum_{j=1}^2 \lambda_j (\widehat{P}_j \widehat{\beta}_j)^{2/\alpha_j} x^{2/\alpha_j}\right\} \mathcal{L}_{I_k}(\mu P_k^{0-1} x^{\alpha_k(1-\tau_k)} (e^t - 1)) dt dx, \quad (15)$$

<sup>1</sup>where  $\text{SNR} = P_k^0 x^{\alpha_k(\tau_k-1)} \sigma^{-2}$  and the Laplace transform of the interference to the  $k^{\text{th}}$  tier is given by

$$\mathcal{L}_{I_k}(s_k) = \exp\left(-2\pi\lambda_k \int_x^\infty \left(1 - \int_0^\infty \frac{\mu}{\mu + s P_k^0 y^{\alpha_k \tau_k} c^{-\alpha_k}} \frac{2\pi\lambda_k}{\mathcal{A}_k} y \exp\left(-\pi \sum_{j=1}^2 \lambda_j (\widehat{P}_j \widehat{\beta}_j)^{\frac{2}{\alpha_j}} y^{\frac{2}{\alpha_j}}\right) dy\right) c dc\right).$$

*Proof:* See Section A of the Appendix. ■

Note that the average ergodic rate  $\mathcal{R}_k$  is the average data rate of a typical UT in the  $k^{\text{th}}$  tier with only one active UT in each cell. Hence, it also denotes the average cell throughput of the  $k^{\text{th}}$  tier when an orthogonal multiple access scheme with round robin scheduling is implemented. Furthermore, the average ergodic rate of a typical randomly located UT in the uplink of a two-tier HetNet can be expressed as

$$\mathcal{R} = \sum_{k=1}^2 \mathcal{A}_k \mathcal{R}_k \quad (16)$$

which simplifies as

$$\mathcal{R} = \sum_{k=1}^2 2\pi\lambda_k \int_0^\infty \int_0^\infty x \exp\left\{-\frac{e^t-1}{\text{SNR}} - \pi \sum_{j=1}^2 \lambda_j (\widehat{P}_j \widehat{\beta}_j)^{2/\alpha_j} x^{2/\alpha_j}\right\} \mathcal{L}_{I_k}(\mu P_k^{0-1} x^{\alpha_k(1-\tau_k)} (e^t - 1)) dt dx. \quad (17)$$

<sup>1</sup>The effect of the realistic association is captured by combining (15) with some empirical formulas (e.g., [35], [36]).

The ergodic rate expression can be simplified for the noise limited network (noise dominates the interference), which is stated as the following corollary of Theorem IV.1.

*Corollary IV.2:* The average ergodic rate in the uplink channel of a typical UT associated with the  $k^{\text{th}}$  tier for the noise limited ( $\sigma^2 \gg I_k$ ) case is given by

$$\mathcal{R}_k = \frac{2\pi\lambda_k}{\mathcal{A}_k} \int_0^\infty -e^\xi \text{Ei}(-\xi) x \exp\left\{-\pi \sum_{j=1}^2 \lambda_j (\widehat{P}_j \widehat{\beta}_j)^{2/\alpha_j} x^{2/\alpha_j}\right\}, \quad (18)$$

where Ei denotes exponential integral function,  $\xi = x^{\alpha_k(1-\tau_k)} P_k^{0-1} \sigma^2$ .

## V. ENERGY EFFICIENCY OF CARRIER-SEPARATED HETNET WITH INTER-FREQUENCY SMALL CELL DISCOVERY

### A. Ideal Average Energy Efficiency

In the previous section we derived generic expressions for the average ergodic rate,  $\mathcal{R}_k$ , and the average power consumption,  $\overline{\mathcal{P}}_{T_k}$ , of the UT in each tier. The ideal AEE in the uplink of HetNet is the ratio of the average bit transmitted by the typical UT to the average energy consumed by the typical UT, while considering the ideal UT association. The average bit transmitted by the typical UT in each tier is obtained from the average ergodic rate and the average time that the typical UT spends in the coverage of each tier, as defined for the ideal association in (4). Given that a typical UT spends an average time  $T_k$  in the coverage of BSs of the  $k^{\text{th}}$  tier, hence the ideal AEE in the uplink of two-tier HetNet can be expressed as

$$\mathcal{C}_J = \frac{\sum_{k=1}^2 T_k \mathcal{R}_k}{\sum_{k=1}^2 T_k \overline{\mathcal{P}}_{T_k}} \quad (\text{bit/J}), \quad (19)$$

where  $T_k$ ,  $\overline{\mathcal{P}}_{T_k}$  and  $\mathcal{R}_k$  are defined in (4), (12) and (15), respectively. Hence, the ideal AEE in the uplink of HetNet given in (19) can be simplified as

$$\begin{aligned} \mathcal{C}_J &= \frac{\sum_{k=1}^2 \mathcal{A}_k \mathcal{R}_k}{\sum_{k=1}^2 \mathcal{A}_k \overline{\mathcal{P}}_{T_k}} \\ &= \frac{\sum_{k=1}^2 \mathcal{A}_k \mathcal{R}_k}{\Delta \sum_{k=1}^2 (\mathcal{A}_k P_k^U) + P_c}. \end{aligned} \quad (20)$$

### B. Realistic Average Energy Efficiency

As mentioned earlier in Section III, the typical UT consumes additional power  $P_m$  for each ISCD that it performs when connected to the macro cell. Hence, this additional power must be incorporated into the power consumption model in order to obtain the realistic AEE of the typical UT in the network. It is important to note that apart from the ISCD performed by the UT when connected to the macro cell, which is for exploiting the traffic offloading opportunities available in the small cell, the UT also performs a radio resource management (RRM) inter-frequency search when its received signal strength falls below a certain threshold [15]. The RRM

inter-frequency search is performed irrespective of the UTs association with either the macro or the small cell with the objective to trigger a handover. This condition arises when the UT is in the cell edge region, where it typically has a lower signal quality. In this work we focus on the additional power consumed by the UT when searching for the small cell with the aim of benefiting from its traffic offloading opportunity, hence we do not consider the RRM inter-frequency search power consumption.

According to the realistic UT association expressions in (5) and (6), the typical UT is connected to the macro cell and small cell for a duration  $\tilde{T}_1 = T(\mathcal{A}_1 + \mathcal{A}_2\mathcal{X})$ , and  $\tilde{T}_2 = (1 - \mathcal{X})\mathcal{A}_2T$ , respectively, where  $\mathcal{X}$  is obtained empirically. Also, given a fixed ISCD measurement duration  $T_m$ , with ISCD periodicity  $V$ , the average number of ISCDs that a typical UT experiences in the coverage of the macro cell can be expressed as

$$\begin{aligned} N_{ISCD} &= \frac{\tilde{T}_1}{T_m + V} \\ &= \frac{T(\mathcal{A}_1 + \mathcal{X}\mathcal{A}_2)}{T_m + V}. \end{aligned} \quad (21)$$

Hence, the average additional energy consumed by the typical UT as a result of the ISCD measurements in the macro cell coverage can be expressed as

$$E_{ifm} = N_{ISCD}T_mP_m \quad (22)$$

$$= \frac{T(\mathcal{A}_1 + \mathcal{X}\mathcal{A}_2)}{T_m + V}T_mP_m, \quad (23)$$

based on the energy consumed for one ISCD measurement, which is given in (7). The AEC of a typical UT in a 2-tier HetNet,  $E_m$ , is thus the sum of the average energy consumed in the first tier (macro coverage), the average energy consumed in searching the small cells, and the average energy consumed in the second tier (small cell coverage). Therefore, the AEC of a typical UT can be expressed as

$$E_m = \sum_{k=1}^2 \tilde{T}_k \bar{P}_{T_k} + E_{ifm}. \quad (24)$$

Consequently, the AEE of a typical UT in the uplink of a carrier frequency separated two-tier HetNet, which incorporates the energy consumed for ISCD process, can be expressed as

$$C_{JC} = \frac{\sum_{k=1}^2 \tilde{T}_k \mathcal{R}_k}{\Delta \sum_{k=1}^2 \left( \tilde{T}_k P_k^U \right) + TP_c + E_{ifm}}, \quad (25)$$

which can be further expressed as

$$C_{JC} = \frac{\mathcal{R}_1(\mathcal{A}_1 + \mathcal{X}\mathcal{A}_2) + \mathcal{R}_2\mathcal{A}_2(1 - \mathcal{X})}{P_1^U(\mathcal{A}_1 + \mathcal{X}\mathcal{A}_2) + P_2^U\mathcal{A}_2(1 - \mathcal{X}) + P_c + \frac{T_mP_m(\mathcal{A}_1 + \mathcal{X}\mathcal{A}_2)}{T_m + V}} \quad (26)$$

after substituting for  $\tilde{T}_k$  and  $N_{ISCD}$ .

## VI. OPTIMAL ISCD PERIODICITY

In this section, we investigate the optimal ISCD periodicity of a typical UT in the uplink of HetNet based on its AEC and AEE. As discussed earlier, there exists scanning frequencies,  $\hat{V}^*$  and  $\hat{V}^{**}$ , that achieves optimal performance in terms of average UT energy consumption and energy efficiency, respectively. If the scanning frequency is less than  $\hat{V}^*$ , the small cells will not be discovered on time hence excessive UT energy consumption due to the time duration in macro cell coverage. On the other hand, excessive energy will be consumed in the search process if the scanning frequency exceed  $\hat{V}^*$ . Similarly, scanning frequency that is less or greater than  $\hat{V}^{**}$  will not be energy efficient, since higher scanning frequency means the small cells will be discovered early thus, high capacity at the expense of excessive UT AEC due to scanning. Whereas, a lower scanning frequency means lower capacity, but with savings in UT AEC as a result of scanning. Hence, for scanning frequency higher than  $\hat{V}^{**}$ , the AEE depreciates due to the excessive power consumption, while the AEE depreciates as a result of the lower rate when the scanning frequency lower than  $\hat{V}^{**}$ .

### A. Approximation of the Percentage of Time a Typical UT Missed Small Cell Offloading Opportunity

In order to obtain the optimal ISCD periodicities in terms of AEC and AEE, i.e.  $V^* = \frac{1}{\hat{V}^*}$  and  $V^{**} = \frac{1}{\hat{V}^{**}}$ , respectively, we must express the percentage of time that a typical UT missed small cell offloading opportunity, i.e.  $\mathcal{X}$ , as a function of ISCD periodicity  $V$ . It can be seen in Fig. 1 that  $\mathcal{X}$  is a function of the ISCD periodicity, the small cell density and the UT speed. Furthermore, it can be observed that  $\mathcal{X}$  can be approximated as a linear function of ISCD periodicity for a fixed UT speed  $\theta = 3$  km/hr and small cell densities  $\lambda_2 = 10\lambda_1$  and  $20\lambda_1$ . However, this is not the case for higher UT speed, hence, we generalize the approximation of  $\mathcal{X}$  as a function of ISCD periodicity  $V$  via a polynomial curve fitting method, for a fixed small cell density and UT speed, as follows

$$\tilde{\mathcal{X}}(V) \approx \mathcal{X}(V) \approx \sum_{f=0}^N a_f V^f, \quad (27)$$

where  $N$  is the order of the polynomial,  $a_f$  is the  $f^{th}$  polynomial coefficient. The parameter  $N$  can be chosen such that the following the mean square error equation is minimized, i.e.  $\varepsilon_0 \ll 1$ ,

$$\frac{\sum_{\mathbf{V}} |\mathcal{X}(V) - \sum_{f=0}^N a_f V^f|^2}{|\mathbf{V}|} \ll \varepsilon_0, \quad (28)$$

where  $|\mathbf{V}|$  denotes the cardinality of the test vector  $\mathbf{V}$ . Table I gives the polynomial order and coefficient for the deployment settings with  $\lambda_2 = 10\lambda_1$  and  $20\lambda_1$ , and  $\theta = 3, 10, 20, 30, 120$  km/hr. Fig. 1 shows a tight match between the exact percentage of time the UT missed small cell offloading opportunity,  $\mathcal{X}$ , and its approximation  $\tilde{\mathcal{X}}$ .

TABLE I  
POLYNOMIAL ORDER AND COEFFICIENTS FOR VARIOUS DEPLOYMENT SETTINGS

Speed	3 km/hr		10 km/hr		20 km/hr		30 km/hr		120 km/hr	
	$10\lambda_1$	$20\lambda_1$	$10\lambda_1$	$20\lambda_1$	$10\lambda_1$	$20\lambda_1$	$10\lambda_1$	$20\lambda_1$	$10\lambda_1$	$20\lambda_1$
$\lambda_2$	1	1	2	2	2	2	3	3	4	4
$N$	1	1	2	2	2	2	3	3	4	4
$a_0$	$-1.27 \times 10^{-4}$	$-1.5 \times 10^{-5}$	$-2.38 \times 10^{-4}$	$-3.55 \times 10^{-4}$	$-1.5 \times 10^{-3}$	$-7.75 \times 10^{-4}$	$-2.440 \times 10^{-3}$	$-9.97 \times 10^{-4}$	$-4.1 \times 10^{-3}$	$-2.718 \times 10^{-3}$
$a_1$	$2.148 \times 10^{-3}$	$1.737 \times 10^{-3}$	$6.987 \times 10^{-3}$	$5.378 \times 10^{-3}$	$1.39 \times 10^{-2}$	$1.156 \times 10^{-2}$	$2.1161 \times 10^{-2}$	$1.5566 \times 10^{-2}$	$8.54 \times 10^{-2}$	$6.633 \times 10^{-2}$
$a_2$	–	–	$-1.28 \times 10^{-5}$	$-1.14 \times 10^{-5}$	$-7.2 \times 10^{-5}$	$-5.71 \times 10^{-5}$	$-1.875 \times 10^{-4}$	$-1.193 \times 10^{-4}$	$-3.3 \times 10^{-3}$	$-2.255 \times 10^{-3}$
$a_3$	–	–	–	–	–	–	$4.8745 \times 10^{-7}$	$3.4865 \times 10^{-7}$	$5.9290 \times 10^{-5}$	$3.7217 \times 10^{-5}$
$a_4$	–	–	–	–	–	–	–	–	$-3.836 \times 10^{-7}$	$-2.3226 \times 10^{-7}$

### B. Optimal ISCD Based on Average Energy Consumption

The average EC expression in (24) can be expressed as a function of the ISCD periodicity as follows

$$E_m(V) = TP_1^U (\mathcal{A}_1 + \mathcal{X}(V) \mathcal{A}_2) + TP_2^U \mathcal{A}_2 (1 - \mathcal{X}(V)) + \frac{TT_m P_m (\mathcal{A}_1 + \mathcal{X}(V) \mathcal{A}_2)}{T_m + V}. \quad (29)$$

By taking  $\mathcal{X}(V) \approx \tilde{\mathcal{X}}(V)$  in (27),  $E_m(V) \approx \tilde{E}_m(V)$ , which is clearly differentiable over its domain, such that  $\frac{\partial \tilde{E}_m(V)}{\partial V}$  can be expressed after simplification as

$$\frac{\partial \tilde{E}_m(V)}{\partial V} = \mathcal{A}_2 \left( \Delta_p (T_m + V)^2 + T_m P_m (T_m + s) \right) \frac{\partial \tilde{\mathcal{X}}(V)}{\partial V} - T_m P_m \left( \mathcal{A}_1 + \mathcal{A}_2 \tilde{\mathcal{X}}(V) \right), \quad (30)$$

where  $\Delta_p = P_1^U - P_2^U$ . Let  $V^*$  be the solution to the equation  $\frac{\partial \tilde{E}_m(V)}{\partial V} = 0$ . Then  $\frac{\partial \tilde{E}_m(V)}{\partial V} \leq 0$  and  $\frac{\partial \tilde{E}_m(V)}{\partial V} \geq 0$  for any  $V \in [0, V^*]$  and  $V \in [V^*, +\infty]$ , respectively, which in turn implies that  $\tilde{E}_m \approx E_m$  decreases over  $V \in [0, V^*]$  and then increases over  $V \in [V^*, +\infty]$ . Consequently,  $E_m(V)$  has a unique minimum, which occurs at  $V = V^*$ . By setting  $\frac{\partial \tilde{E}_m(V=V^*)}{\partial V} = 0$  and using the approximation of  $\mathcal{X}(V)$ , for a given speed and small cell density given in Table I in (30), we can obtain  $V^*$ . For the case where  $\mathcal{X}(V)$  is linear, i.e. the polynomial order  $N = 1$  in (27), the optimal ISCD search based on the AEC can be simplified as

$$V^* = -T_m + \sqrt{\frac{T_m P_m [\mathcal{A}_2 (a_0 - a_1 T_m) + \mathcal{A}_1]}{\mathcal{A}_2 a_1 \Delta_p}}. \quad (31)$$

However, for the case where the polynomial order,  $N > 1$ , we simply use a linear search method such as Newton-Raphson method.

### C. Optimal ISCD Based on UT's Average Energy Efficiency

The optimal ISCD periodicity in the previous subsection was based on the UT's AEC. In this subsection, we derive the optimal ISCD based on the AEE expression of (26), which can be expressed as a function of the ISCD periodicity as follows

$$\mathcal{C}_{J_C}(V) = \frac{\mathcal{R}_1 (\mathcal{A}_1 + \mathcal{X}(V) \mathcal{A}_2) + \mathcal{R}_2 \mathcal{A}_2 (1 - \mathcal{X}(V))}{P_1^U (\mathcal{A}_1 + \mathcal{X}(V) \mathcal{A}_2) + \frac{T_m P_m (\mathcal{A}_1 + \mathcal{X}(V) \mathcal{A}_2)}{T_m + V} + P_2^U \mathcal{A}_2 (1 - \mathcal{X}(V))}. \quad (32)$$

Similar to the AEC case, the AEE is differentiable over its domain and the ISCD periodicity that maximizes the AEE,

TABLE II  
SYSTEM PARAMETERS.

Parameter	Symbol	Value (units)
Bandwidth per tier	$W$	20 MHz
Macro cell BS density	$\lambda_1$	$\frac{1}{\pi 400^2 m^2}$
Small cell BS density	$\lambda_2$	$5\lambda_1, 10\lambda_1, 20\lambda_1$
UT density	$\lambda^{(u)}$	$100\lambda_1$
Macro cell BS transmit power	$P_1$	46 dBm
Small cell BS transmit power	$P_2$	26 dBm
Small cell Bias factor	$\beta_2$	0, 2, 4, 6, 8, 10 dB
UT pathloss compensation factor	$\tau_1 = \tau_2 = \tau$	0, 0.2, 0.4, 0.6, 0.8, 1.0
UT power control parameter	$P_1^0 = P_2^0 = P^0$	-50 dBm
Reference pathloss	$L_0$	-38.5 dB
Pathloss exponent	$\alpha_k$	3, 3.5, 4
Thermal noise density	$N_0$	-174 dBm/Hz

$V^{**}$ , can be obtained by setting  $\frac{\partial \tilde{\mathcal{C}}_{J_C}(V=V^{**})}{\partial V} = 0$ , which simplifies as

$$\begin{aligned} \frac{\partial \tilde{\mathcal{C}}_{J_C}(V=V^{**})}{\partial V} &= 0 \\ &= \tilde{E}_m(V) \mathcal{A}_2 (\mathcal{R}_1 - \mathcal{R}_2) \frac{\partial \tilde{\mathcal{X}}(V)}{\partial V} \\ &\quad - \left( \sum_{k=1}^2 \mathcal{A}_k \mathcal{R}_k + (\mathcal{R}_1 - \mathcal{R}_2) \mathcal{A}_2 \tilde{\mathcal{X}}(V) \right) \frac{\partial \tilde{E}_m(V)}{\partial V} \end{aligned} \quad (33)$$

Note that the optimal ISCD periodicity based on AEC, i.e.  $V^*$ , and AEE, i.e.  $V^{**}$ , are equivalent when the ergodic rate in both tiers are equal, since  $\frac{\partial \tilde{\mathcal{C}}_{J_C}(V=V^{**})}{\partial V} = \frac{\partial \tilde{E}_m(V)}{\partial V}$  in (33), when  $\mathcal{R}_1 = \mathcal{R}_2$ .

## VII. NUMERICAL RESULTS AND DISCUSSIONS

In this section, we present numerical results on the ergodic rate, AEC, AEE and the optimal ISCD periodicity of a typical UT in the uplink of a 2-tier HetNet with both tiers operating on separate carrier frequencies. The system parameters are given in Table II.

### A. Achievable rate

We obtain numerical results for the average ergodic rate (in Theorem IV.1) with respect to the main system parameters; pathloss exponent, power control factor, BS density and bias factor. In Fig. 2, we compare average ergodic rate obtained via simulation with the analytical results. We plot the average ergodic rate as a function of the small cell bias factor,  $\beta_2$ , for small cell density values of  $\lambda_2 = 5$ , pathloss values  $\alpha_1 = \alpha_2 = 3.5$  and power control factors,  $\tau_1 = \tau_2 = 0.8$  and  $\tau_1 = \tau_2 = 0$ . The results in Fig. 2 clearly show that the analytical results provide lower bounds to the average ergodic rate. Furthermore, increasing the small cell bias factor,  $\beta_2$ , leads to a reduction in the average ergodic rate of a typical

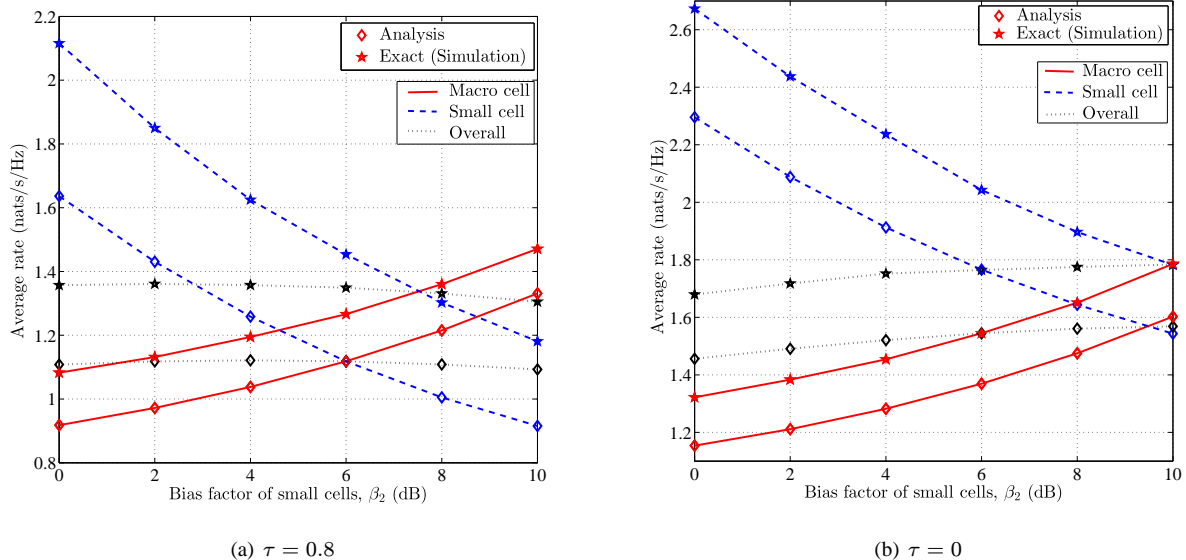


Fig. 2. Average ergodic rate for varying bias factor of small cells in a 2-tier HetNet,  $\beta_1 = 1$ ,  $\lambda_1 = \frac{1}{\pi 400^2 \text{m}^2}$ ,  $\lambda_2 = 5\lambda_1$ ,  $P_1 = 46$  dBm,  $P_2 = 26$  dBm

UT in the small cell whereas the average ergodic rate of the typical UT in the macro cell increases. This is due to the fact that as the small cell bias factor increases, the coverage area of the small cells increases leading to increase in the interference suffered by the typical UT and consequently a reduction in the achievable ergodic rate. As the small cell bias factor increases, more macro UTs with low SINR become associated with the small cell, which degrades the average ergodic rate of the typical UT in the small cell, but improve the rate in the macro cell.

In Fig. 3, using the analytical results, we plot the average ergodic rate of a typical UT as a function of the power control factor,  $\tau_1 = \tau_2 = \tau$ , for pathloss exponents  $\{\alpha_1 = 3.5, \alpha_2 = 3.5\}$ ,  $\{\alpha_1 = 3.5, \alpha_2 = 3\}$  and  $\{\alpha_1 = 3, \alpha_2 = 3.5\}$ , small cell BS density  $\lambda_2 = 10\lambda_1$  and no bias, i.e.,  $\beta_1 = \beta_2 = 1$ . The results show that the lowest ergodic rate in a tier is achieved by the tier with the lowest pathloss exponent, whereas the contrary holds for the tier with the highest pathloss exponent. This is because the signal from the interfering cells will be stronger with lower pathloss exponent and weaker with higher pathloss exponent i.e., interference decays more slowly as pathloss exponent increases. It can be further observed that the ergodic rate of a typical UT over each tier and over the entire network reduces with increasing power control factor  $\tau$ . Since the obtained rate is for typical UT in the network, the effect of the power control factor on all UTs (i.e., low, medium and high SINR UTs) is combined into a single value. Therefore, the decrease in the average rate as  $\tau$  increases is due to the loss in rate of some UTs whose transmit power is reduced, but the effect of this reduction is not overcome on average by the reduction in interference and increased rate by other UTs. Note that this observation was also made for the single tier network in [37].

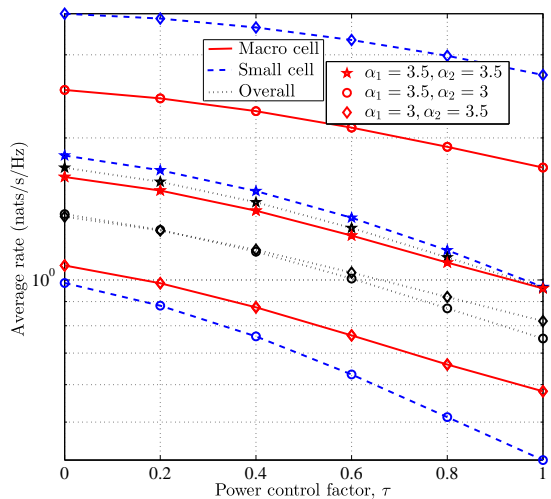


Fig. 3. Average ergodic rate in a 2-tier HetNet as a function of fractional power control parameter  $\tau$ , for bias factor  $\beta_1 = \beta_2 = 1$ ,  $\lambda_1 = \frac{1}{\pi 400^2 \text{m}^2}$ ,  $\lambda_2 = 10\lambda_1$ ,  $P_1 = 46$  dBm and  $P_2 = 26$  dBm.

### B. UT Power Consumption

In Fig. 4, we plot the average UT transmit powers in each tier against the small cell bias factor,  $\beta_2$ , for UT power control,  $\tau = 1$  and  $\tau = 0.8$ . It can be observed that significant reduction in transmit power is achieved when the UT connects to the small cell compared to when it connects to the macro cell, in the case with full power control, i.e.,  $\tau = 1$ . This is as a result of the reduced distance to the BS when typical UT is in the coverage of the small cell, hence a lower transmit power is required to achieve a desired received signal. As the power control factor reduces, the transmit power becomes more independent of the distance between the nodes, hence



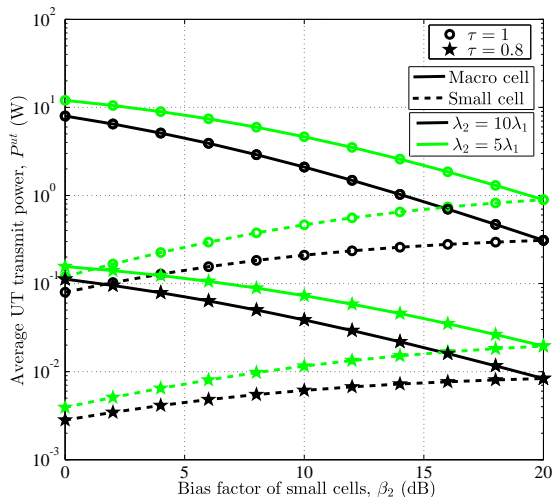


Fig. 4. Average user transmit power for varying bias factor of small cells in a 2-tier HetNet,  $\beta_1 = 1$ ,  $\lambda_1 = \frac{1}{\pi 400^2 \text{m}^2}$ ,  $\lambda^{(u)} = 100\lambda_1$ ,  $P_1 = 46$  dBm,  $P_2 = 26$  dBm, and  $\alpha_1 = \alpha_2 = 3.5$ .

a reduction in the ratio of the average UT transmit power in the macro cell to that in the small cell. The result also shows that as expected, the average transmit power in the small cell increases as the small cell bias factor increase, whereas the contrary holds in the macro cell.

### C. Average Energy Efficiency

The results presented in Sections VII-A and VII-B clearly shows the rate gain and transmit power reduction that is achieved when the UT connects to the small cell of an inter-frequency HetNet. This section presents numerical results on the AEE while considering both the ideal and realistic UT association. Furthermore, the average ergodic rate used in evaluating the AEE is based on the analytical results.

1) *Ideal Average Energy Efficiency*: In Fig. 5, we plot the ideal AEE, which is based on the ideal UT association against the small cell bias factor. It can be seen that increasing the density of small cells lead to an increase in the UT's AEE in the macro cell, small cell and overall network. Furthermore the UT's AEE performance in the small cell depreciate as the bias factor increases, since the average rate of the typical UT in the small cell decreases while its transmit power increases as the small cell bias factor increases, as shown in Figs. 2 and 4. On the other hand, the performance of the macro cell improves since the contrary occurs. It can also be observed that contrary to the overall average ergodic rate in Fig. 2, the overall AEE in a fully loaded network improves with increase in bias factor.

2) *Realistic Energy Efficiency*: In Fig. 6, we plot the realistic AEE against the small cell discovery periodicity. In the upper graph, typical UT speed 3 km/hr, 20 km/hr, and 120 km/hr are considered for small cell density  $\lambda_2 = 10\lambda_1$ . The results clearly show that there exists an ISCD periodicity that maximizes the AEE. The lower graph shows the AEE performance for small cell densities,  $\lambda_2 = 10\lambda_1$ ,  $\lambda_2 = 20\lambda_1$

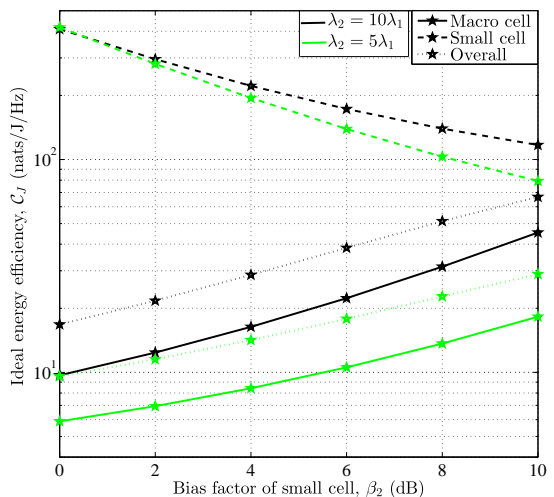


Fig. 5. Ideal AEE for varying bias factor in a 2-tier HetNet,  $\beta_1 = \beta_2 = 1$ ,  $\lambda_1 = \frac{1}{\pi 400^2 \text{m}^2}$ ,  $\lambda_2 = 5\lambda_1, 10\lambda_1$ ,  $P_1 = 46$  dBm,  $P_2 = 26$  dBm  $\tau = 0.8$  and  $\alpha_1 = \alpha_2 = 3.5$ .

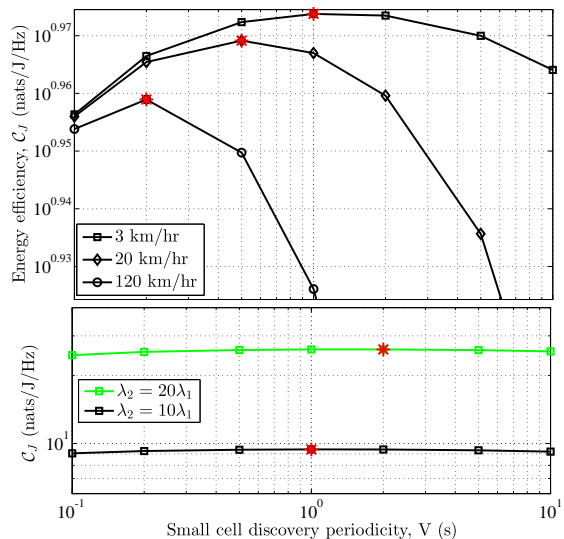


Fig. 6. Realistic AEE for varying small cell discovery periodicity and UT speed,  $\beta_1 = \beta_2 = 1$ ,  $\lambda_1 = \frac{1}{\pi 400^2 \text{m}^2}$ ,  $\lambda_2 = 10\lambda_1$ ,  $P_1 = 46$  dBm,  $P_2 = 26$  dBm,  $\tau = 0.8$  and  $\alpha_1 = \alpha_2 = 4$ . The star marker indicates the ISCD periodicity that achieves the optimal AEE.

and typical UT speed of 3 km/hr. As it is expected, increasing the density of the small cells leads to an increase in AEE, since this results in a reduction in the average transmit power of the typical UT coupled with an improvement in the small cell traffic offloading. Furthermore, it can be seen that the optimal ISCD periodicity is dependent on the density of small cells and speed of the typical UTs. For a fixed small cell density,  $\lambda_2$ , a lower small cell discovery periodicity is required to achieve the maximum AEE as the typical UT speed increases. Whereas for a fixed speed of the typical UT, as the small cell density increases, the optimal ISCD periodicity required to achieve the maximum AEE also increases.

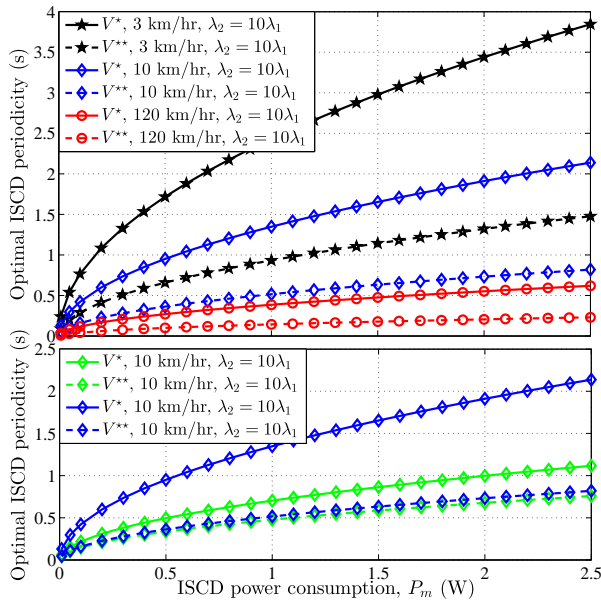


Fig. 7. Optimal ISCD periodicity for various ISCD power consumption, small cell densities,  $\lambda_2 = 10\lambda_1, 20\lambda_1$ , and UT speed of 3, 10, 120 km/hr, UT transmit powers,  $P_1^U = 1.6114$  W and  $P_2^U = 1.14$  W.

Thus this analysis and subsequent determination of optimal ISCD periodicity can pave the way towards the design of self organizing network (SON) [38] functions that can adapt the cell discovery periodicity with respect to particular environment (UT speed and small cell density) to achieve optimal AEE performance. Its worth noting that in future HetNets, small cell densities might change impromptu as cell may be switched off and on in order to improve the networks energy efficiency. Hence, the need for such adaptive algorithms that exploits the existence of optimal ISCD for given cell density becomes even stronger.

#### D. Optimal ISCD Periodicity

The results presented in this section are based on a full power control implementation in both tiers, i.e.  $\tau_1 = \tau_2 = 1$ . In Fig. 7, we plot the optimal ISCD periodicity for ISCD power consumption  $P_m$  ranging from 0.01 W to 2.5 W, average UT transmit power in the macro cell  $P_1^U = 1.6114$  W, which corresponds to  $P_1^0 = -69$ dBm, UT speed  $\theta = 3, 10$  and 120 km/hr, and small cell density  $\lambda_2 = 10\lambda_1$  and  $20\lambda_1$ . The average UT transmit power in the small cells with density  $\lambda_2 = 10\lambda_1$  and  $\lambda_2 = 20\lambda_1$  at  $P_2^0 = -50.5$  dBm are 1.14 W and 0.5 W, respectively. The upper graph shows the impact of varying of UT speed on the optimal ISCD periodicity, while the lower graph shows the impact of varying the small cell density. The upper graph clearly shows that as the UT speed increases, the ISCD periodicities required to achieve optimal AEC and AEE performances reduces. On the other hand, the lower graph shows that increasing the small cell density reduces the ISCD periodicities required to achieve optimal AEC and AEE performances. Furthermore, Fig. 7 clearly shows that increasing the ISCD power results

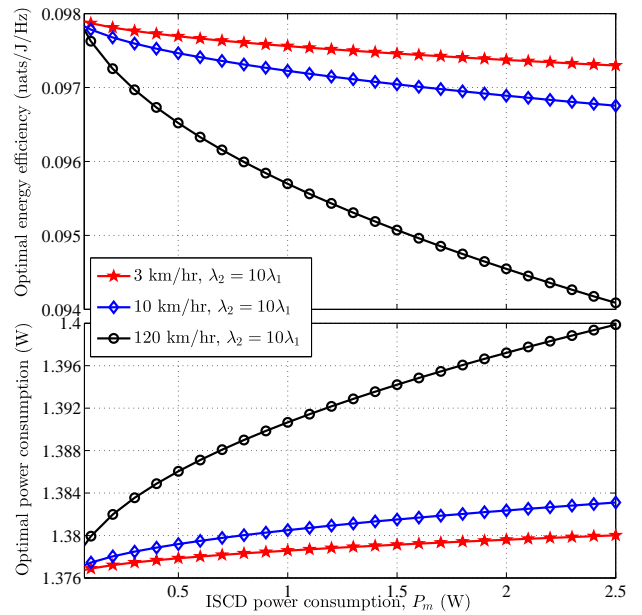


Fig. 8. Average power consumption and AEE based on optimal ISCD periodicity, for small cell density,  $\lambda_2 = 10\lambda_1$ , and UT speed of 3, 10, 120 km/hr, UT transmit powers,  $P_1^U = 1.6114$  W and  $P_2^U = 1.14$  W.

in an increase in the ISCD periodicity required to achieve the optimal performance in terms of both AEC and AEE. Though UT power consumption is lower when UT is connected to the small cell, however, additional power is spent in searching the small cell. Hence increasing the ISCD power implies an increase in the search periodicities required to achieve optimal AEC and AEE performances. Fig. 7 further shows that for a fixed UT transmit power in the small cell, the ISCD periodicity required to achieve optimal AEC performance exceeds the ISCD periodicity required to achieve optimal AEE performance.

In Fig. 8, we plot the average UT power consumption (lower graph) and AEE (upper graph) based on the optimal ISCD periodicity against the ISCD power consumption,  $P_m$ , for small cell density  $\lambda_2 = 10\lambda_1$  and UT speed  $\theta = 3, 10$  and 120 km/hr. As expected, increasing the ISCD power leads to an increase in the average power consumption and a reduction in the AEE. In addition, with the same network parameters, a high speed UT is less energy efficient since higher scanning frequency (i.e., lower ISCD periodicity) is required to attain optimal performance.

In Fig. 9, we plot the percentage reduction in AEC (lower graph) and the percentage increase in AEE (upper graph), respectively, that are achieved from using the optimal ISCD periodicity over using sub-optimal ISCD periodicity  $V = 0.04, 0.1, 10$  and 60 s. We plot both graphs for average UT transmit power  $P_2^U$  in the small cell ranging from 0.01 W to 1.44 W, which corresponds to  $P_2^0$  ranging from  $-69.5$  dBm to  $-49.5$  dBm, and average UT transmit power in the macro cell  $P_1^U = 1.6114$  W, which corresponds to  $P_1^0 = -69$ dBm. Fig. 9 shows that significant amount of energy can be saved by adopting the optimal ISCD periodicity especially when

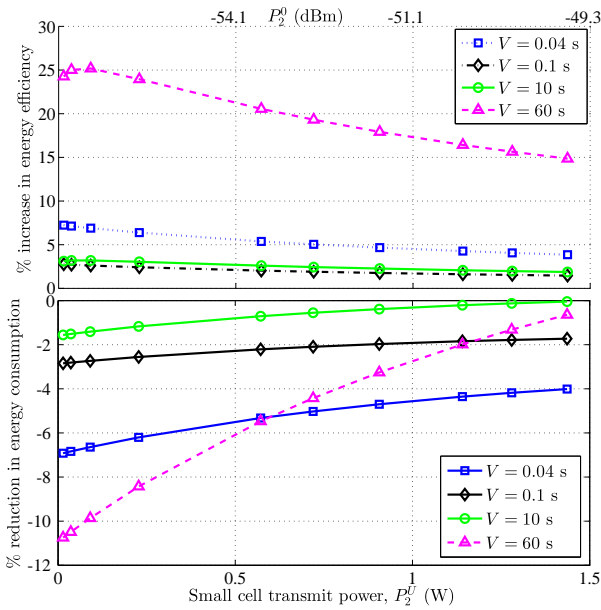


Fig. 9. Percentage reduction in AEC and percentage increase in AEE achieved by using optimal ISCD periodicity over sub-optimal ISCD periodicity, for small cell densities,  $\lambda_2 = 10\lambda_1$ , UT speed,  $\theta = 10$  km/hr, ISCD power,  $P_m = 1$  W and UT transmit power,  $P_1^U = 1.6114$  W ( $P_1^0 = -69$  dBm).

there is a large deviation between the optimal and sub-optimal values. For example, the optimal ISCD periodicity for deployment setting with  $\lambda_2 = 10\lambda_1$ ,  $P_m = 1$  W,  $P_2^U = 1.14$  and UT speed of 10 km/hr used in Fig. 9 is such that  $V^* \wedge V^{**} \in [0.5 \ 1.5]$  s (as shown in Fig. 7). However, using ISCD periodicity  $V = 0.04$  and 60 s results in larger difference compared with  $V = 0.1$  and 10 s, which are more closer to the optimal values.

Since, optimal ISCD periodicity can be calculated as function of statistical UT speeds and small cell density only, optimal ISCD periodicity can be maintained in a spatio-temporally varying environment of a HetNet by designing appropriate SON functions, without incurring major overheads in terms of hardware redesign or signaling overheads. As the energy limited nature of UT is one of the major challenges in future broadband networks such as 5G, the significant gain in the AEE of the UT through the implementation of optimal ISCD periodicity can increase the battery life of UT significantly, particularly in ultra-dense HetNets that are being deemed as necessary in 5G landscape.

### VIII. CONCLUSION

In this paper, we have investigated the energy efficiency of the user terminal in the uplink of a carrier frequency separated two-tier heterogeneous network with flexible cell association, also known as biasing. Using Poisson point process (PPP) our system model captured the network topology and the design parameters associated with each tier including base station transmit power, density, bias factor, and power control factor. We first derived generic expressions for the average transmit power and average ergodic rate, which were later used in

energy efficiency derivation. The energy efficiency expressions are based on the ideal and realistic user terminal associations. In the former, user terminals associate with the base station with the maximum biased received signal without considering the overheads required for such association. On the other hand, the latter further incorporates the percentage of time that a typical user terminal missed small cell offloading opportunity as a result of the periodicity of the measurement conducted for small cell discovery. In addition to this, the additional power consumed by the user terminal due to the inter-frequency small cell discovery (ISCD) measurement was also included for the later.

The main findings of this paper can be summarized as follows: Firstly, there exists ISCD periodicity that maximizes the energy efficiency and minimizes the energy consumption when the realistic user terminal association is considered. Secondly, significant savings in the energy consumption of the user terminal can be achieved by using the optimal ISCD periodicity. Lastly, the optimal ISCD periodicity for the user terminal based on energy efficiency always differs from that which is based on energy consumption, as long as the average ergodic rate in both tiers differs. Hence, the user terminals ISCD periodicity should be chosen based on the target objectives such as energy consumption minimization or energy efficiency maximization. The findings of this paper can be implemented in real network through self-organizing network functions being already adapted by 3GPP for emerging cellular networks, where the periodicity of the ISCD process can be selected based on the environmental setting to obtain the optimal energy efficiency performance.

Note that randomly distributed network architecture has been presented in this paper. However, future network architectures will be clustered and not randomly distributed. Since accurate modeling of network architecture is crucial, hence a better modeling such as Matérn process with repulsion deserves much attention in future study.

### APPENDIX

#### A. Proof of Theorem IV.1

From (14), the average uplink ergodic rate in the  $k^{th}$  tier is

$$\begin{aligned} \mathcal{R}_k &= \int_0^\infty \mathbb{E}_{\text{SINR}_k} [\ln(1 + \text{SINR}_k(x))] f_{X_k}(x) dx \\ &= \frac{2\pi\lambda_k}{\mathcal{A}_k} \int_0^\infty \mathbb{E}_{\text{SINR}_k} [\ln(1 + \text{SINR}_k(x))] \\ &\quad x \exp \left\{ -\pi \sum_{j=1}^K \lambda_j \left( \hat{P}_j \hat{\beta}_j \right)^{2/\alpha_j} x^{2/\alpha_j} \right\} dx \quad (34) \end{aligned}$$

where  $f_{X_k}(x)$  is defined in (2). Given that  $\mathbb{E}[X] = \int_0^\infty \mathbb{P}[X > x] dx$  for  $X > 0$  hence, we obtain

$$\begin{aligned} \mathbb{E}_{\text{SINR}_k} [\ln(1 + \text{SINR}_k(x))] &= \int_0^\infty \mathbb{P}[\ln(1 + \text{SINR}_k(x)) > t] dt \\ &= \int_0^\infty \mathbb{P}[\text{SINR}_k(x) > e^t - 1] dt \quad (35) \end{aligned}$$

The SINR in (13) can be rewritten as  $\gamma(x) = \frac{h_k}{P_0^{-1} x^{\alpha_k(1-\tau_k)} Q}$ , where  $Q = I_k + \frac{\sigma^2}{L_0}$ . Hence,

$$\begin{aligned} & \mathbb{E}_{\text{SINR}_k}[\ln(1 + \text{SINR}_k(x))] \\ &= \int_0^\infty \mathbb{P}[h_k > P_0^{-1} x^{\alpha_k(1-\tau_k)} Q (e^t - 1)] dt \quad (36) \end{aligned}$$

However,

$$\begin{aligned} & \mathbb{P}[h_k > P_0^{-1} x^{\alpha_k(1-\tau_k)} Q (e^t - 1)] \\ &= \int_0^\infty \exp[-\mu x^{\alpha_k(1-\tau_k)} P_k^{0^{-1}} (e^t - 1) q] f_Q(q) dq \\ &= \mathbb{E}_Q \left[ \exp\left(-\mu x^{\alpha_k(1-\tau_k)} P_k^{0^{-1}} (e^t - 1) q\right) \right] \\ &= \exp\left(-\frac{e^t - 1}{\text{SNR}}\right) \mathbb{E}_{I_k} \left[ \exp\left(-\mu x^{\alpha_k(1-\tau_k)} P_k^{0^{-1}} (e^t - 1) I_k\right) \right], \\ &= \exp\left(-\frac{e^t - 1}{\text{SNR}}\right) \mathcal{L}_{I_k}(\mu x^{\alpha_k(1-\tau_k)} P_k^{0^{-1}} (e^t - 1)) \quad (37) \end{aligned}$$

where  $\text{SNR} = \frac{P_0^0 x^{\alpha_k(\tau_k - 1)}}{\sigma^2}$  and  $\mathcal{L}_{I_k}(s_k) = \mathbb{E}_{I_k}[e^{-s I_k}]$  is the laplace transform of  $I_k$  which simplifies as

$$\begin{aligned} & \mathcal{L}_{I_k}(s_k) \\ &= \mathbb{E}_{I_k} \left[ \exp\left(-\sum_{z \in \mathcal{Z}_k} s P_k^0 Y_z^{\alpha_k \tau_k} V_z^{-\alpha_k} h_z\right) \right] \\ &= \mathbb{E}_{Y_z, V_z, h_z} \left[ \prod_{z \in \mathcal{Z}} \exp(s P_k^0 Y_z^{\alpha_k \tau_k} V_z^{-\alpha_k} h_z) \right] \\ &\stackrel{(a)}{=} \mathbb{E}_{Y_z, V_z} \left[ \prod_{z \in \mathcal{Z}} \mathbb{E}_{h_z} [\exp(s P_k^0 Y_z^{\alpha_k \tau_k} V_z^{-\alpha_k} h_z)] \right] \\ &\stackrel{(b)}{=} \mathbb{E}_{V_z} \left[ \prod_{z \in \mathcal{Z}} \mathbb{E}_{Y_z} \left[ \frac{\mu}{\mu + s P_k^0 Y_z^{\alpha_k \tau_k} V_z^{-\alpha_k}} \right] \right] \\ &\stackrel{(c)}{=} \exp\left(-2\pi\lambda_k \int_x^\infty \left(1 - \mathbb{E}_{Y_z} \left[ \frac{\mu}{\mu + s P_k^0 Y_z^{\alpha_k \tau_k} c^{-\alpha_k}} \right] \right) c dc\right), \quad (38) \end{aligned}$$

where (a) is due to the independence of  $h_z$ , (b) follows from the fact that the interference fading power  $h_z \sim \exp(\mu)$  and (c) is given in [23]. The limits of the integration are from  $x$  to  $\infty$ . Since  $x$  is the distance between the typical UT and its serving BS, the closest interferer is at least a distance  $x$  from the serving BS of the typical UT. Similar to [37], considering that each BS is randomly located in the Voronoi cell of its corresponding active UT while assuming orthogonal multiple access within each cell. Hence, the PDF of the distance between an interfering UT to its serving BS, i.e.,  $Y_z$  can be approximated by the PDF  $f_{X_k}(x)$  of the distance  $X_k$  between a typical UT and its serving BS in the  $k^{\text{th}}$  tier given in (2). Hence by applying the density of  $Y_z$ , the Laplace transform of the interference in the  $k^{\text{th}}$  tier given in (38) can be further expressed as follows

$$\begin{aligned} \mathcal{L}_{I_k}(s) &= \exp\left(-2\pi\lambda_k \int_x^\infty \left(1 - \int_0^\infty \frac{\mu}{\mu + s P_k^0 y^{\alpha_k \tau_k} c^{-\alpha_k}} \frac{2\pi\lambda_k}{\bar{A}_k} \right. \right. \\ &\quad \left. \left. y \exp\left(-\pi \sum_{j=1}^K \lambda_j \left(\hat{P}_j \hat{\beta}_j\right)^{\frac{2}{\alpha_j}} y^{\frac{2}{\alpha_j}}\right) dy\right) c dc\right). \quad (39) \end{aligned}$$

Finally, the average ergodic rate expression in (15) is obtained by substituting (37) into (36) and thereafter substituting the later into (34).

#### ACKNOWLEDGMENT

We would also like to acknowledge the support of the University of Surrey 5GIC (<http://www.surrey.ac.uk/5gic>) members for this work.

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